This paper provides a unified analysis for the onset of the 1998 financial crisis and the strong economic recovery afterward in Russia and other former Soviet Union countries. Before the crisis a banking failure arose owing to the coexistence of a lemons credit market and high government borrowing. In a lemons credit market low credit risk firms switched from bank to nonbank finance, including trade credits and barter trade, generating an externality on banks’ interest rates. The collapse of the treasury bills market in the financial crisis triggered a change in banks’ lending behavior, providing initial conditions for banking development.

JEL Classification Numbers: G3, G21, P34, O16, D82

Keywords: banking development, institutional trap, financial crisis

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I. INTRODUCTION

After the collapse of the Soviet Union, Russia, Ukraine and other former Soviet Union countries took a bumpy road in their transition to a market economy. The real sectors of these economies experienced a sharp contraction in 1998, output was only around 50 percent of its 1989 level (see Table 1). During the period of 1989 to 1998, the real sector had accumulated a huge amount of outstanding debt and arrears and noncash payments had become a dominant feature of these economies. Taking Russia as an example, total payables to the enterprise sector exploded from around 20 percent of GDP in 1994 to over 70 percent of GDP in 1998, while total receivables rose from 20 percent of GDP to about 45 percent of GDP over the same period. Associated with these phenomena, noncash payments and barter started to rise from 8 percent in 1994, when inflation was under control, to more than 50 percent of sales in 1998 (see Figure A1).

<table>
<thead>
<tr>
<th>Country</th>
<th>Real GDP (1989 = 100)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CIS</td>
<td>54</td>
</tr>
<tr>
<td>Russia</td>
<td>55</td>
</tr>
<tr>
<td>Ukraine</td>
<td>37</td>
</tr>
<tr>
<td>Azerbaijan</td>
<td>44</td>
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<tr>
<td>Belarus</td>
<td>78</td>
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<tr>
<td>Kazakhstan</td>
<td>61</td>
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<tr>
<td>Central Europe</td>
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<tr>
<td>Poland</td>
<td>117</td>
</tr>
<tr>
<td>Czech Republic</td>
<td>93</td>
</tr>
<tr>
<td>Hungary</td>
<td>95</td>
</tr>
</tbody>
</table>

In contrast to the contraction of the real sector, the number of commercial banks in these economies increased rapidly. In Russia, the number of commercial banks increased from fewer than 100 in 1988 to about 2,400 in 1994 and 2,500 in 1998.\(^3\) Many

\(^3\) Although the number of banks has increased dramatically, the Russian banking sector is still quite concentrated. In 1997, the top five banks accounted for 36 percent, and the top 50 banks for 71 percent, of total assets. About three-quarters of all household deposits were maintained with Sberbank.
of those banks are owned by large firms. Despite the boom in the number of banks and their cross holdings in the real sector, banks failed to lend to firms, and banks’ credit to the real sector declined substantially in these economies. For example, in real terms, Russian bank credits to the real sector declined by almost 60 percent, while the ruble loan interest rates were very high (Table 2).

<table>
<thead>
<tr>
<th>Year</th>
<th>Total Loans</th>
<th>Foreign Currency</th>
<th>Ruble Loans</th>
<th>Interest Rates 1)</th>
<th>Inflation 2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1996</td>
<td>247</td>
<td>117</td>
<td>130</td>
<td>146.8</td>
<td>47.7</td>
</tr>
<tr>
<td>1997</td>
<td>310</td>
<td>130</td>
<td>180</td>
<td>32.0</td>
<td>14.7</td>
</tr>
<tr>
<td>1998</td>
<td>422</td>
<td>298</td>
<td>123</td>
<td>41.8</td>
<td>27.7</td>
</tr>
<tr>
<td>1999</td>
<td>597</td>
<td>304</td>
<td>293</td>
<td>39.7</td>
<td>85.7</td>
</tr>
<tr>
<td>2000</td>
<td>956</td>
<td>368</td>
<td>588</td>
<td>24.4</td>
<td>20.8</td>
</tr>
<tr>
<td>2001</td>
<td>1418</td>
<td>474</td>
<td>944</td>
<td>17.9</td>
<td>21.5</td>
</tr>
</tbody>
</table>

Source: International Monetary Fund, Central Bank of Russia

1) Commercial banks’ 3-months lending rates in percent
2) Consumer price index in percent

Why did banks refuse to lend to firms? Where did commercial banks invest instead? Evidence shows that they concentrated their investments in treasury bills. For example, by the end of 1997, commercial banks in Russia invested almost three-quarters of ruble deposits in federal government securities. A similar picture emerges from other FSU countries, notably Ukraine (Table 3). In fact, Russian and Ukrainian banks are among the worst performers in transition countries in terms of mobilizing savings and allocating credit to the private sector, and they are a key factor underlying the surge of nonbank finance, including trade credit and barter trade, in these economies. The irony is that even bank owners in these economies chose nonbank financing for their manufacturing and trade, while letting banks absorb credit from these large firms.

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4 In nominal terms ruble loans to the real sector declined by 31.7 percent, from 180 billion rubles to 123 billion rubles, between 1997 and 1998.

and invest in government bonds. Both countries experienced a continued decline over time in the scale of banking activities with respect to the real sector. After the massive privatization, the ratio of credit to the private sector declined from 12 percent of GDP in 1994 to 8 percent in 1997 in Russia, and from 5 percent in 1994 to 2 percent in 1997 in Ukraine. By contrast, the average ratio for all the transition countries was 22 percent of GDP in 1994 and 23 percent in 1997.

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</thead>
<tbody>
<tr>
<td>Azerbaijan</td>
<td>-</td>
<td>1</td>
<td>-</td>
<td>3</td>
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<tr>
<td>Belarus</td>
<td>18</td>
<td>7</td>
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<td>10</td>
</tr>
<tr>
<td>Kazakhstan</td>
<td>25</td>
<td>6</td>
<td>5</td>
<td>9</td>
</tr>
<tr>
<td>Latvia</td>
<td>16</td>
<td>7</td>
<td>11</td>
<td>-</td>
</tr>
<tr>
<td>Lithuania</td>
<td>18</td>
<td>11</td>
<td>10</td>
<td>10</td>
</tr>
<tr>
<td>Russia</td>
<td>12</td>
<td>7</td>
<td>8</td>
<td>12</td>
</tr>
<tr>
<td>Ukraine</td>
<td>5</td>
<td>1</td>
<td>2</td>
<td>9</td>
</tr>
<tr>
<td>Czech Republic</td>
<td>40</td>
<td>57</td>
<td>68</td>
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<tr>
<td>Hungary</td>
<td>26</td>
<td>22</td>
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</tr>
<tr>
<td>Poland</td>
<td>12</td>
<td>16</td>
<td>18</td>
<td>19</td>
</tr>
</tbody>
</table>

Table 3. Credit to the Private Sector in Transition Countries
(in percent of GDP)

Source: International Monetary Fund, *International Financial Statistics* (Washington), various issues

Given the poor economic performances of Russia and Ukraine, it is not surprising that a financial crisis occurred in 1998. However, the very fast and strong recoveries in Russia and Ukraine after the 1998 financial crisis caught many observers by surprise. In 1999, Russia and Ukraine experienced positive growth for the first time since the fall of the Soviet Union. The IMF, in its World Economic Outlook, adjusted its forecast of economic growth for Russia upward several times. Russian GDP grew by 3.2 percent in 1999, 7.5 percent in 2000, and 5 percent in 2001; and 4.4 percent growth was expected in 2002. Similarly, in Ukraine, GDP growth was 5.9 percent in 2000 and 9.1 percent in 2001; and the economy was expected to grow by 5.0 in 2002 (see Figure A3). Total arrears and barter have started to decline in Russia. In particular, barter and noncash payments dropped by 20 percent in 1999 and continued to decline in 2000 and 2001.
(see Figure A1). Even more interesting is the fact that commercial banks started to lend to the real sector after the crisis. Ruble loans to the economy more than doubled in nominal terms between 1998 and 1999 from 123 billion rubles to 293 billion rubles. At the same time, lending rates of commercial banks declined sharply in nominal as well as real terms (see Table 2 and Figure A1). A similar picture emerges for Ukraine, where bank credit to the private sector increased from 2 percent of GDP in 1997 to 9 percent of GDP in 1999 (see Table 3 and Figure A1).

These observations on Russia and Ukraine before and after the 1998 financial crisis seem puzzling. First, although the number of banks increased substantially, arrears and barter started to explode in Russia after 1994, when macroeconomic stabilization was in place. Thus, the banks’ failure to lend to the real sector and the noncash economy do not appear to be a consequence of hyperinflation. Second, following the outbreak of the financial crisis in 1998 that brought down many banks, arrears and barter started to decline. This is not what one would expect, because a financial crisis usually causes widespread liquidity shortages and often leads to a credit crunch, forcing firms to run up more arrears and engage in more barter transactions. Third, immediately after the financial crisis, Russia and Ukraine started to have substantial economic growth for the first time since the collapse of the U.S.S.R. This stands in contrast to the experience of many other economies, for which financial crises have led to sharp output decline.

These puzzles raise many question. What explains the separation between the financial and the real sectors before the crisis? What is the relationship between the noncash economy, on the one hand, and the exuberance in financial markets, on the other hand? How can we explain the unexpected high growth of the Russian and Ukrainian economies after the 1998 financial crisis? Has the unexpected growth something to do with the decline in barter trade and the increase in bank lending to the real sector? If so, what is the function of a financial crisis in this process?

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According to the interfax news agency the share of barter in sales dropped as well in Ukraine from 33 percent in 1999 to 17 percent in 2000, and to 8 percent in 2001. The Russian Economic Barometer estimates that noncash payments have dropped to below 10 percent at the beginning of 2003.

Due to the collapse of the government treasury bills market, the large exposure of portfolios of commercial banks to this market made many banks insolvent. This has led to a consolidation and concentration in the banking sector with 3 state banks (of which one is Sberbank) now accounting for about 80 percent of the assets. Moreover, Sberbank started to aggressively enter the lending market pushing some of the existing large banks out of this market. For the restructuring of the Russian banking sector after the crisis, see Interfax Center for Economic Analysis, Russia's Largest Banks in 1999, Moscow 1999.

Based on a sample of 195 crisis episodes across 91 developing countries, Gupta, Mishra and Sahay (2003) find in their study on output responses to financial crisis that around 60 percent of the crises have been contractionary. Moreover, Loayza, and Ranciere (2001) find in the countries that experience a fall in output after crisis, that it takes on average 4 years for output to recover.
We develop a model to address the above questions. Our model assumes severe information asymmetry in these economies, so that banks are not able to distinguish good credit risk firms from bad ones. Thus, banks charge high interest rates on loans to all borrowing firms. This, in turn, induces good-quality firms to turn to nonbank finance, such as trade credits and barter trade, which involves less of information asymmetry but are more costly.\(^9\) The option for good firms to raise liquidity through nonbank finance drives up bank lending interest rates further, since banks expect that only lower-quality firms will borrow. In equilibrium, then only low-quality firms borrow from banks while good-quality firms turn to nonbank finance, and the banking sector looks for high-yield government securities in which to invest. We call this a banking trap, in the sense that the financial sector is separated from the real sector of the economy. This separation hinders banking sector development and economic growth, although on the surface there is financial exuberance, particularly in the government securities market. Using data from a survey among firms in Ukraine in 1997, our empirical evidence suggests that bank loans were mainly allocated to firms of low quality.

Our theory thus highlights the role of the financial sector before and after the crisis.\(^10\) It suggests a link between the government’s budget deficit and the noncash economy which has been overlooked so far. In our model, the government’s public debt and the size of the noncash economy are simultaneously determined. It is frequently argued that arrears and barter in Russia and Ukraine are driven by tax motives. By allowing firms to hide some of their profits, thereby lowering their taxable income, nonbank finance is seen to contribute to the difficulty of raising taxes and thus causing the government’s budget to explode. Our theory suggests, in addition, that the government’s budget deficit is crowding out bank lending to the real sector by creating an environment in which banks invest in the treasury bills market, which

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\(^9\) In our model, we take the existence of non-bank finance for firms as given and focus on the banking failure. In a recent paper Marin and Schnitzer (2003) argue that barter is a response to a banking failure. Barter is a trade credit between firms which is repaid in goods rather than cash. Marin and Schnitzer take the banking failure as given and argue that barter offers a deal-specific collateral which effectively lowers credit enforcement costs.

\(^10\) For insightful discussions of the role of the financial sector in economic transition, see Berglof and Bolton (2002).
offers exceptionally high returns, and the real sector turns to nonbank finance to meet its liquidity needs.\textsuperscript{11} \textsuperscript{12}

Our theory also offers an explanation of why the 1998 crisis has had some beneficial effects for the economies of Russia and Ukraine. Our explanation links the puzzling facts that following the crisis of 1998 the noncash economy started to decline in Russia and Ukraine, the banking sector started to lend to the real sector and loan interest rates declined sharply. When the Russian government defaulted on its bonds in August 1998, the securities market collapsed. Although many banks with large holdings of government securities collapsed, the economy turned around, moving from negative growth to positive growth. We argue that the vanished market for government bonds induced the surviving banks to reallocate their assets to the real sector at lower interest rates to attract borrowers. Lower loan interest rates, in turn, made it attractive for some better-quality firms to start borrowing from banks rather than to continuing to use nonbank finance. This improved the average creditworthiness of the pool of borrowers and, in turn, further lowered interest rates and induced more firms to switch from barter trade to bank loans. The strong economic recovery naturally followed, and also provided an opportunity for the banking sector to further develop.\textsuperscript{13} Based on data for 20 transition countries, we test the prediction that the financial crisis was a trigger for more rapid long-run economic growth and banking development. Our evidence shows that before the crisis, the allocation of bank credit to the real sector of the economy was, indeed, hampered by the government's overissuing of bonds and by the opportunities firms had to engage in barter trade, but after the crisis, banks started to provide more loans to firms at low interest rates.

\textsuperscript{11} In the debate over the non-cash economy tax reasons figure prominently as an explanation. However, empirical evidence for Russia and Ukraine suggests that tax motives have only minor importance, while the lack of liquidity and high borrowing costs for bank loans are the prime motivation for firms to engage in barter trade, see Commander and Mumssen (1999) for evidence in Russia, and Marin, Kaufmann, Gorochowskij (2000) for evidence in Ukraine.

\textsuperscript{12} According to Shleifer and Treisman (2000) this was the price Russia had to pay to achieve stabilization of inflation. Rather than printing money to finance the budget, the government issued treasury bills and maintained artificially high interest rates on these bills to co-opt the banks who heavily invested in this market. Yields on the GKO market reached up to 60 percent (see Figure 1).

\textsuperscript{13} During the crisis the ruble depreciated by more than fifty percent (see Figure A3) which may be an alternative explanation for why barter dropped after the August crisis in Russia. However, Ukraine had only a mild depreciation of the exchange rate but also experienced a sharp drop in barter and arrears after 1998. This suggests that some other force is at work here. Similar arguments also apply to oil prices after 1998 given Russia is an oil exporter while Ukraine is an oil importer. Another alternative argument that the return to the cash economy in Russia is due to a reversal in capital flight after the August crisis does not seem to be supported by the data. Westin (2000) and Loungani and Mauro (2000) argue that capital flight picked up again in Russia after the tightening of capital controls in the aftermath of the crisis.
The rest of the paper is organized as follows. In Section II, we develop a model of the bank-firm relationship in a “lemons market” à la Akerlof (1970). In Section III, we characterize the equilibrium of the lemons market in which the financial and the real sectors are separated. Section IV describes how the financial crisis has helped the economies of the CIS countries and the Baltics to get out of the banking trap. In Section V, we test the predictions of the model with firm-level data from Ukraine. Section VI concludes. All proofs are provided in Appendix II.

II. Model

We consider an economy with $M$ banks and $N$ firms, where $N > M$; and the government.

Firms: Firm $i$’s ($i = 1, ..., N$) quality, measured as its probability of being solvent, $\lambda_i$, is only known to itself. The quality of firms can be ranked as $\lambda_1 > \lambda_2 > ... > \lambda_N$. But the ranking of firms is not known to any particular bank and firm in the market. The average quality of all firms is $\bar{\lambda}_N = \frac{1}{N} \sum_{i=1}^{N} \lambda_i$, which is known to all the firms and banks. The liquidity demand of firms can be met through borrowing from banks or through other means, such as borrowing from other firms in the form of trade credits in cash or in the form of trade credits in goods (barter trade)\textsuperscript{14}. We will call these alternative forms of finance as nonbank-financing (NBF). To meet their liquidity needs profit maximizing firms choose the cheaper way between bank financing and NBF.

To simplify the analysis we assume that NBF cost $b$ is constant.\textsuperscript{15} NBF cost $b$ is a reduced form capturing many possible interpretations.\textsuperscript{16}

Government: We suppose that the government’s total revenue equals its tax revenue plus its borrowing and NBF firms evade taxes.\textsuperscript{17} Given the possibility for tax

\textsuperscript{14} Overdue trade credits in cash (firm arrears) and trade credits in goods (barter) exploded in Russia and other FSU economies. Usually goods used in barter are not fixed assets and heterogeneous in quality. This means that these goods are typically not collaterizable assets for bank loans due to high cost of quality assessment or selling for banks. For barter as a collateralized trade credit, see Marin and Schnitzer (2002).

\textsuperscript{15} This assumption can easily be relaxed without changing the qualitative results. For example, one could make $b$ to depend on firm characteristics like the firm’s level of quality. However, as will become clear later this complication would reinforce the separation result we will derive in the next section without adding insight.

\textsuperscript{16} In addition to solving liquidity problems, it is argued that NBF may cut costs since it may reduce hold-up or disorganization problems (Marin and Schnitzer, 2003); may help firms in tax evasion (for empirical evidence, see Commander and Mumssen, 1999; and Marin, Kaufmann, Gorochowskij, 2000).

\textsuperscript{17} Although in our model NBF is driven by financial considerations, NBF offers better opportunities for firms to evade taxes. This is confirmed well with the empirical evidence for Russia and other FSU countries (see Commander and Mumssen, 1999; and Marin, Kaufmann, Gorochowskij, 2000).
evasion, the government is assumed not to be able to collect taxes effectively. For any given government revenue, $R$, the lower the tax revenue, $T$, the more the government issues bonds to finance its expenditures $B = R - T$.

When there are $n$ NBF firms the tax revenue is reduced to $T = (N - n)t$, where $t$ is the tax paid by each firm. To borrow more, the yield of government bond, $s$, has to be higher. To capture this idea in a simple way, we assume that the yields of government bonds, $s$, is a positive linear function of the amount of borrowing. When there is no tax evasion the interest rate of government securities reaches its lower bound with $s = \phi r_0$, where $\phi$ is the investors’ relative confidence in government securities. When the relative confidence in government securities is the same as that of investing in the private sector, then $\phi = 1$; otherwise it is $\phi > 1$. To make things simple, we treat $\phi$ as a reduced form and take $\phi$ and $t$ as exogenously given.

To summarize, we have the government security yield equation, which is a function of the number of NBF firms in the economy,

$$s(n) = r\phi \frac{B(n)}{B} = r\phi \frac{R - (N - n)t}{R - Nt}$$

where, $\bar{B}$ is planned government borrowing; and $B(n)$ is realized government borrowing.

Bank-firm relationship: We assume free entry in the banking sector. Facing competition, each bank makes its investment decision based on expected returns. If the expected return of investing in government securities is higher than that of lending to a firm, banks will invest in government securities rather than lend to firms; and vice-versa.

We suppose that there is asymmetric information between banks and firms such that banks are not able to identify which firm is of good quality and which is of bad quality. Asymmetric information between banks and firms is a severe problem in transition economies. Most banks in transition economies are new and have very little experience with credit evaluation. Furthermore, the lack of accounting standards and market valuation of firms’ assets makes it difficult to evaluate firms’ creditworthiness. The only information that banks are assumed to have is the average quality of the firms in the economy, $\lambda_N$. Thus, banks’ ex ante belief of the probability that a firm will be able to repay its loan is $\lambda_N$. Therefore, banks’ expected rate of return of lending to firms is $r_N\lambda_N$, where $r_N$ is the rate of repayment of a solvent firm when there are in

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18 The government can either issue government bond domestically with a high yield; or borrow from foreign investors by issuing dollar denominated bonds and paying higher interest rates.

19 Alternatively, $\phi$ may also be interpreted as a risk premium on government securities.
total \( N \) firms borrowing. Comparing the expected rate of return of lending to a firm and investing in government securities, the arbitrage condition for a bank is

\[
(1 + r_N) \bar{\lambda}_N = 1 + s.
\]

Or the rate that a bank will charge to a firm will be

\[
r_N = (1 + s)/\bar{\lambda}_N - 1.
\]

Facing this rate, \( r_N \), a firm \( i \) with a probability of success of \( \lambda_i \), will face an expected marginal cost of borrowing from the bank of

\[
\lambda_i(1 + r_N) = (1 + s)\frac{\lambda_i}{\bar{\lambda}_N}.
\]

If raising liquidity through NBF is less costly than borrowing from banks, firm \( i \) will borrow from other firms. The condition for this to happen for firm \( i \) is then

\[
\frac{\lambda_i}{\bar{\lambda}_N} \geq \frac{b}{1 + s}.
\]

Thus, we have,

**Lemma 1** Firm \( i \) will use NBF if and only if:

\[
\lambda_i \geq \frac{b\lambda_N}{1 + s}. \tag{1}
\]

Notice that \( \frac{b}{1 + s} \) is the ratio between and the cost of raising $1 liquidity through NBF and the yields of government bonds, which also affects the cost of raising $1 liquidity through a bank loan. From Lemma 1, obviously, a firm is more likely to use NBF to solve its liquidity constraint, when the marginal cost of NBF \( b \), is low, or the interest rate charged by banks, \( s \), is high. Moreover, the higher is the quality of a firm, \( \lambda_i \), the more likely it engages in NBF. The intuition of this result is straightforward. With information asymmetry between banks and firms, banks charge an interest rate according to the market average quality. As a result the high quality borrowers subsidize
the low quality borrowers in the pool of different quality borrowers. Turning to NBF helps this high quality firms to escape to subsidize the low quality firms.

III. Separation of the Financial and the Real Sector

In the previous section, we have shown that in a lemons lending market good quality firms face higher borrowing costs than bad quality firms. As a result good quality firms are more likely to use NBF to solve their liquidity problems than to borrow from banks. Moreover, as better quality firms switch to NBF to meet their liquidity problems, it generates an externality on the lending rates of banks, because the average quality of the pool of borrowing firms is lowered. Consequently the lending interest rate goes up, which in turn leads more better quality firms to turn away from banks. This logic repeats until in equilibrium only the bad quality firms borrow from banks and the good quality firms raise liquidity through NBF. That is, in equilibrium the financial sector is separated from the real sector of the economy. In the following we show this separating equilibrium formally.

First, we illustrate conditions for a separating equilibrium between the financial and real sector when $s$ is exogenously given. We then derive a separating equilibrium with $s$ being endogenized. To make things simple, we assume that $\lambda_i = \lambda_{i-1} - \mu$ for all $i = 1, 2, \ldots, N$, and $\lambda_N = \mu$.

Associated with this assumption, for a given $\mu$, $N$ can be interpreted as a measure of heterogeneity of the firms, which determines information asymmetry. When $N$ is large, the degree of information asymmetry between firms and banks in the economy is high, and subscript $i$ now can be interpreted as a label for a group of firms that have the same quality $\lambda_i$. Under this assumption, the average quality of all firms is

$$\bar{\lambda}_N = \frac{1}{N} \sum_{i=1}^{N} \lambda_i = \frac{(1 + N)\mu}{2}.$$

The firms’ quality can be ranked as $\lambda_1 > \lambda_2 > \ldots \lambda_{n-1} > \lambda_n > \ldots > \lambda_N$. We assume that the ranking is not known to any agent in the economy. Let us suppose that $\lambda_n$ satisfies the following condition,

$$\lambda_{n-1} > \frac{b\bar{\lambda}_N}{1 + s} > \lambda_n.$$
According to Lemma 1, this condition implies that firms with subscript $i \leq n - 1$ will not borrow from banks because their cost of borrowing is too high. All other firms with $i \geq n$ will find it cheaper to borrow from banks. Thus, at the starting point the $n - 1$ high quality firms do not borrow from banks.

In the following lemma (proof in Appendix II), we show for exogenously given $s$ that when the bank lending market is a lemons market, in equilibrium the higher the ratio $\frac{1+s}{b}$, the fewer firms will borrow from banks.

**Lemma 2** There are three possible equilibria in a lemons bank lending market: 1). if $1 \leq \frac{1+s}{b}$, the equilibrium is $n^* = N$ and no firm borrows from banks; however; 2) if $\frac{N+2}{2(N+1)} \geq \frac{1+s}{b}$, the equilibrium is $n^* = 0$ and all firms borrow from banks; and finally, 3). if $\frac{N+2}{2(N+1)} < \frac{1+s}{b} < 1$, there exists an equilibrium $n^* \in (0, N)$ such that all firms with subscript $i \leq n^*$ do not borrow, while all the remaining $N-n^*$ firms borrow from banks.

Lemma 2 shows that in a bank lemons lending market with sufficiently high yields of government securities $s$ relative to the NBF costs $b$ in equilibrium no firm will borrow from banks and the financial sector is separated from the real sector. However, if the ratio between the treasury bill rates and NBF costs is sufficiently low, all firms will borrow from banks. At a moderate ratio, low quality firms only will borrow from banks.

So far we have assumed that the yields of government bonds $s$ is exogenously given. However, $s$ will depend also on the number of NBF firms in the economy. In the following, we endogenize the yields of government bonds $s$ to make its value depends on the number of NBF firms in the economy. Substituting $s(n)$ into the condition in Lemma 1, the no-borrow condition becomes

$$s(n) \geq \psi(n)$$  \hspace{1cm} (2)

with

$$s(n) = \phi r_0 \left( 1 + \frac{t}{R - N t} \right)$$

as the government securities yields equation; and

$$\psi(n) = \frac{b(N-n+2)}{2(N-n+1)} - 1$$
as the banking lemons market equation. The following proposition (proof in Appendix II) gives conditions for a separating equilibrium in which the good quality firms do not borrow from banks.\textsuperscript{20}

\textbf{Proposition 1} If \((b - 1) \left(1 - \frac{tN}{R}\right) > \phi r_o > \frac{b(N+2)}{2(N+1)} - 1\), a unique interior equilibrium \(n^* \in (0, N), s^* \in (\phi r_o, \frac{\phi r_o R}{R-Nt})\) exists such that \(n^*\) better quality firms do not borrow and the remaining \(N - n^*\) low quality firms borrow from banks. Moreover, the equilibrium value of \(n^*, s^*\) increase with \(t, \phi r_o\) and decrease with \(R\).

Intuitively, when the number of NBF firms increases, the government’s tax revenue \(T\) declines, which in turn pushes up the yields of government bonds, \(s\). This, in turn, may lead more firms not to borrow from banks. The switching from borrowing to NBF will generate a negative externality on other borrowing firms who may stop borrowing as well. As a consequence \(s\) is pushed further up which will again induce more firms not to borrow. This cycle repeats until \(s\) is too high to attract more borrowers; or the borrowing firms are of too poor a quality to switch to NBF.

The above result illustrates a banking trap. Banks invest in government bonds, while firms, in particular good quality ones, solve their liquidity problems through NBF. The economy is stuck in the banking trap which causes a separation between the real sector and the banking sector. This separation result between the real and the banking sector is substantially different from a conventional ‘government crowding out’ story because information asymmetry is one of the key factors which cause the separation.

The following example illustrates that when the degree of information asymmetry increases, the separation between the two sectors becomes stronger. In our simulation we ‘calibrate’ the model with data from Russia in 1997 before the August financial crisis. The total government expenditure in percent of GDP in Russia was 18.4\% in 1997. Thus we choose 18\% for \(R\). Since planned tax revenue \(T\) is not observable we assume a value of 10 for \(T\). With respect to the value of the exogenous benchmark lending rate \(r\), we use an average lending rate of Czech commercial banks, which were among the best established banks in transition economies, between 1997 (13.2\%) and 1999 (8.7\%), which was 10\%.

Example1: NBF and Information Asymmetry. We consider two economies which differ in the degree of information asymmetry between banks and firms but share all other parameter values with \(r = 0.10, \phi = 1.5, b = 2.1, R = 18, T = 10\).

\textsuperscript{20} The result shows only the case that is most relevant to our evidence. A full characterization of the equilibria of the model is available upon request.
Case 1: Moderate degree of information asymmetry: \( N = 10 \). Figure 1 gives the resulting NBF equation \( \psi(n) \), which is defined in the proof of Proposition 3.2 and the government security yield equation \( s(n) \). The intersection of the two equations gives the equilibrium at point \( T \) at which 61 percent of the firms do not borrow from banks and the government security rate \( s \) settles at 26 percent. In Russia in 1997 more than 50 percent of firms’ sales were financed by other firms in the form of barter transactions and the treasury bills market rate reached 28 percent (see Figures A1 to A3). Thus, for reasonable parameter values the model is quite consistent with the data for Russia in 1997.

![Figure 1: Moderate Information Asymmetry](image)

Case 2: High degree of information asymmetry: \( N = 160 \). Figure 2 gives the corresponding NBF equation \( \psi(n) \) and government security yield equation \( s(n) \). At the new equilibrium at point \( T \) 98 percent of the firms are involved in NBF and the treasury bill rate reaches 33.4 percent.

The example illustrates that an economy with a higher degree of information asymmetry suffers from a stronger separation between the real sector and the banking sector. By contrast, a conventional crowding out story would not depend on the degree of information asymmetry between banks and firms as is the case here.
IV. Financial Crisis and Banking Development

In the previous section we have derived an equilibrium in which the financial sector is separated from the real sector and the yields of government securities $s$ are high. In this section we analyze how an exogenous shock in the agents confidence in the government which is triggered by the government’s default and the fire sale of government securities affects an economy with separated financial and real sectors.

A strong negative confidence shock, i.e. an exogenous negative shock in $\phi$ creates a substantial drop in the yields of government securities $s$. As a result, the banks which are heavily invested in government securities will suffer major losses. The immediate effect of such a financial crisis on the real sector is, however, limited when the two sectors are separated.

**Corollary 1** With the separation between the banking sector and the real sector, the plunge of $\phi$ has no immediate impact on the number of good quality firms $n^*$ which do not borrow from banks, although banks may make losses.

Typically, a financial crisis leads to a sharp fall in GDP followed by a slow and gradual recovery, as observed in crises in Latin America in the 1980s and in Nordic countries in the 1990s. In an economy in which the financial and the real sectors are separated, however, a financial crisis may be beneficial for the economy. When $\phi$, thus $s$ plunge, banks' options outside of the real sector disappear. This induces banks

---

21 To make the model simple, we choose to treat the financial crisis as an exogenous event. Our analysis focuses on the consequences of a financial crisis.

22 See footnote 6.
to lower lending interest rates to attract more firms. As a result, some good quality firms switches back to borrowing from banks, and the average quality of borrowers further improves. The improved quality of the borrowing pool further lowers bank lending rates, and thus inducing more good-quality firms to borrow. Moreover, when more good-quality firms borrow, the tax revenue goes up. This reduces government borrowing, which leads to a further drop in \( s \). This logic leads to a new equilibrium in which better-quality firms borrow from banks; loan interest rates go down; and banks invest less in government securities. The ‘separation’ syndrome disappears if the shock is strong.

Starting from an economy where \( n^* \) good quality firms use NBF, we show now in the following proposition (proof in Appendix II) that the banking sector gets to reconnect with the real sector when \( \phi \) drops.

**Proposition 2** If the banking sector is separated from the real sector in an economy, a financial crisis caused by a plunge of \( \phi \) may lead to an integration of the two sectors. In the new equilibrium, the ‘separation’ syndrome may diminish or even disappear associated with a substantial lower lending rate.

Starting from an economy where \( n^* \) good quality firms use NBF, we show now in the following proposition (proof in Appendix II) that the banking sector gets to reconnect with the real sector when \( \phi \) drops.

Our result is consistent with what has happened in Russia. The financial crisis in Russia was triggered by the default of the government. Investors lost their confidence in government securities and the treasury bond market collapsed. Any bank that had survived this big shock needed to change its portfolio dramatically and started to lend to the real sector at much lower lending interest rates than before the crisis. Comparing bank lending to the private sector in 1997, the year before the financial crisis, with that in 2000, reveals an increase in bank lending in Russia and in Ukraine from 8 percent and 2 percent of GDP, respectively, to 12 percent and 9 percent of GDP, respectively, while barter trade declined by about 30 percent.

It is important to point out that although the financial crisis can destroy the bad equilibrium associated with a banking trap, it only provides the initial conditions for banking development. This is because severe information asymmetry is the key factor which causes the separation between the real sector and the banking sector. As long as information asymmetry between banks and firms is severe, a financial crisis may not be a sufficient trigger to pull the economy out of a banking trap. Indeed, the following example illustrates that when the degree of information asymmetry is large enough, the lemons market problem is so serious that a financial shock is not enough to pull the economy out of a banking trap.

**Example 2:** The Impact of Financial Crisis on Banking Development and the Role of Information Asymmetry. We look at two economies with the same parameter
values as in the previous example (‘calibrated’ to Russian data before the crisis) given by $r = 0.10$, $b = 2.1$, $T = 10$, $R = 18$. The initial value of confidence into government securities is the same, $\phi = 1.8$. The only difference between the two economies is assumed to be the degree of information asymmetry.

Case 3: Moderate degree of information asymmetry: $N = 10$. Figure 3 gives the $\psi(n)$ curve and the lines $s(n)$ and $s'(n)$ before and after, respectively the financial crisis hits the economy. Before the shock ($\phi = 1.8$) the equilibrium settles at point $T$ at which 74 percent of the firms are involved in NBF with a government security rate of 34.8 percent. After the shock (a drop in $\phi$ to 1.2), in the new equilibrium no firm engages in NBF and the treasury bill rate is 12 percent.

![Figure 3: Moderate Information Asymmetry](image)

Case 4: High degree of information asymmetry: $N = 160$. Figure 4 gives the $\psi(n)$ curve with three lines before the shock $s(n)$, after a moderate shock $s'(n)$, and finally after a drastic shock $s''(n)$. Before the shock, the economy settles at an equilibrium $T$ at which 98.8 percent of the firms engage in NBF and the government security rate is 40 percent. With the same moderate shock as in Figure 3 (captured by a drop in $\phi$ from 1.8 to 1.2) the new equilibrium at $T'$ still gives 97.6 percent of firms involved in NBF and a treasury bill rate of 12.1 percent. Only with a drastic drop of $\phi$ from 1.8 to 0.3 is the NBF economy removed and no firm barter trades with a government security rate of 3 percent.

The example illustrates that a small confidence shock in government securities is sufficient to bring an economy out from the separation between the real sector and the banking sector if the degree of information asymmetry is moderate. However, a large shock is required to do the same for an economy with a high degree of information asymmetry. The example demonstrates how the financial shock interacts with the
degree of information asymmetry and thus highlights the relative importance of each factor for banking development.

![Figure 4: High Information Asymmetry](image)

V. Empirical Evidence

We first examine the predictions of our model on the behavior of firms when there is a high degree of information asymmetry between firms and banks; and when there is a high level of government borrowing. Our investigation is based on data of about 100 firms which engaged in barter trade in Ukraine in 1997. We interviewed 55 firms to obtain information on 165 barter deals. Each firm provided us with 3 barter deals. Each barter deal involved 2 firms, a seller and a buyer. Many of the firms were well informed about the financial and economic conditions of the firms they traded with because they served as financiers. Table 4 and Table 6 give descriptive statistics of the variables used in the empirical analysis.\(^\text{23}\)

Our model predicts that low quality firms will predominantly finance their production with bank loans. We examine the relationship between bank lending and the characteristics of firms in Table 5. In the table we run the regressions for all firms in the sample (first four columns) and then for firms with positive bank debt only. We use the firms’ bank debt in percent of sales DEBT as the dependent variable. 62 percent of the firms have positive bank debt with an average ratio of bank debt to firms sales of \(6.3\) percent (see Table 6). As a measure for the firms’ quality \(\lambda_i\) we use the variable WAGEARREARS. WAGEARREARS is a proxy for the firms’ quality, since a firm which stops paying its workers must be in desperate financial and economic conditions. The more indebted the firm is vis-a-vis its workers the less likely it is that the firm

\(^{23}\) For a more detailed description of the data sample see Marin, Kaufmann, Gorochowskij (2000).
will be able to repay its bank loans and thus the larger the banks' credit risk. Thus, our theory predicts a positive sign on the WAGEARREARS variable. Turning to the results it appears that WAGEARREARS is significant and positive in all specifications.

Table 4. Bank Lending and Firm Characteristics

<table>
<thead>
<tr>
<th></th>
<th>bank debt in percent of sales</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0 - 105</td>
</tr>
<tr>
<td></td>
<td>100%</td>
</tr>
<tr>
<td>BARTCOST</td>
<td>mean</td>
</tr>
<tr>
<td></td>
<td>Anova:F-test</td>
</tr>
<tr>
<td></td>
<td>sign. level</td>
</tr>
<tr>
<td>TOT</td>
<td>mean</td>
</tr>
<tr>
<td></td>
<td>Anova:F-test</td>
</tr>
<tr>
<td></td>
<td>sign. level</td>
</tr>
<tr>
<td>WAGEARREARS</td>
<td>mean</td>
</tr>
<tr>
<td></td>
<td>Anova:F-test</td>
</tr>
<tr>
<td></td>
<td>sign. level</td>
</tr>
<tr>
<td>EMPLOY</td>
<td>mean</td>
</tr>
<tr>
<td></td>
<td>Anova:F-test</td>
</tr>
<tr>
<td></td>
<td>sign. level</td>
</tr>
</tbody>
</table>

Source: Data Sample of 165 Barter Deals in Ukraine in 1997

Next, we include BARTCOST and TOT as variables capturing the NBF cost. BARTCOST is an index which takes the value of zero if the firms output is produced with only one input and approaches one when the firm uses several inputs from other sectors. We use BARTCOST here as a measure of the cost of raising liquidity via barter. When a firm trades in many inputs it will have more leverage in barter trading between varieties of goods and thus will have lower bartering cost. We expect a negative coefficient on BARTCOST. Turning to the results BARTCOST is negative and significant suggesting that firms with higher barter costs borrow more from banks.

---

24 Blanchard and Kremer (1997) use the same variable as a measure for the hold-up problems of firms. The larger the number of inputs used for production the more complex the production and the more bargaining problems arise. In their theory of barter Marin and Schnitzer (2003) suggest lower bartering costs for firms with more complex production. They argue that barter trade helps firms to deal with the hold-up problem.
Table 5. Determinants of Bank Lending to Firms

<table>
<thead>
<tr>
<th></th>
<th>all firms</th>
<th></th>
<th>firms with bank debt</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(1)</td>
<td>(2)</td>
<td>(3)</td>
<td>(4)</td>
</tr>
<tr>
<td>( \ln(\text{WAGEARREARS}) )</td>
<td>0.988</td>
<td>0.959</td>
<td>0.955</td>
<td>0.952</td>
</tr>
<tr>
<td></td>
<td>(0.000)</td>
<td>(0.000)</td>
<td>(0.000)</td>
<td>(0.000)</td>
</tr>
<tr>
<td>( \ln(\text{BARTCOST}) )</td>
<td>-5.237</td>
<td>-5.163</td>
<td>-5.144</td>
<td>-5.144</td>
</tr>
<tr>
<td></td>
<td>(0.000)</td>
<td>(0.000)</td>
<td>(0.000)</td>
<td>(0.000)</td>
</tr>
<tr>
<td>TOT</td>
<td>0.033</td>
<td>0.033</td>
<td>0.033</td>
<td>0.033</td>
</tr>
<tr>
<td></td>
<td>(0.051)</td>
<td>(0.051)</td>
<td>(0.051)</td>
<td>(0.051)</td>
</tr>
<tr>
<td>STATED</td>
<td>-0.099</td>
<td>-0.121</td>
<td>-0.321</td>
<td>0.074</td>
</tr>
<tr>
<td></td>
<td>(0.817)</td>
<td>(0.814)</td>
<td>(0.814)</td>
<td>(0.814)</td>
</tr>
<tr>
<td>( \ln(\text{EMPLOY}) )</td>
<td>0.011</td>
<td></td>
<td></td>
<td>-0.204</td>
</tr>
<tr>
<td></td>
<td>(0.938)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( R^2 ) Adj</td>
<td>0.353</td>
<td>0.375</td>
<td>0.368</td>
<td>0.360</td>
</tr>
<tr>
<td>( N )</td>
<td>86</td>
<td>86</td>
<td>86</td>
<td>86</td>
</tr>
</tbody>
</table>

OLS - regressions; \( p \) - values in parentheses
Source: Data Sample of 165 Barter Deals in Ukraine in 1997

\( \text{WAGEARREARS} = \) wage arrears in percent of sales
\( \text{BARTCOST} = \) index which takes the value of zero if the firm trades with only one other firm, and which tends to one if the firm trades with many firms
\( \text{TOT} = \text{SCASH} - \text{PCASH} \)

\( \text{SCASH} \) is the difference between the barter price and cash price in percent of the cash price for the trade credit side of the barter deal.
\( \text{PCASH} \) is the difference between the barter price and cash price in percent of the cash price for the goods payment side of the barter deal.
\( \text{STATED} = \) dummy variable with value 1 when the firm is state owned
\( \text{EMPLOY} = \) firm's number of employees
Furthermore, we include the variable TOT into the regression which captures the terms of trade effect of barter. We will use it here as a measure for the credit costs of barter. TOT measures in percent the extent to which barter shifts the terms of trade in favor of the firm extending a trade credit within barter. The larger the shift in the terms of trade the more costly it is to raise liquidity via barter trade. For given costs for bank loans an increase in the credit costs of barter induces firms to switch to bank loans to solve their liquidity needs and thus we expect a positive sign on the TOT variable. TOT turns out to be positive and highly significant at conventional levels.

Lastly, we introduce the variables STATED and EMPLOY to control for ownership and firm size. One possible reason why the bad quality firms receive more bank loans than other firms is that the bad firms may be state owned and/or large. State owned firms or large firms may have better creditworthiness because of the expectation of a state bail out. It turns out, however, that neither STATED nor EMPLOY are significant at conventional levels in the all firms regressions. In the regressions for firms with positive bank debt (last four columns) STATED is not significant and firm size appears to hinder the firm to get loans (the relationship is significant and negative).

VI. Conclusions and Policy Implications

We have developed a model that explains both the onset of the financial crisis in 1998 and the striking economic recovery afterward in Russia and other former Soviet
Union economies. Before the crisis, the economies of Russia and Ukraine were stuck in a banking trap in which banks failed to lend to the real sector and firms raised liquidity through nonbank finance, because of the coexistence of a lemons credit market and the government’s overissuance of bonds to finance its budget gap. Despite the financial exuberance on the surface, banking development was seriously hampered and the economic performance was poor. The collapse of the treasury-bill market triggered the financial crisis, which brought down many banks and destroyed the surviving banks’ investment opportunities in government securities. As a result, the surviving banks started to lend to the real sector at low interest rates, which induced more good-quality firms to use low-cost bank loans rather than costly nonbank finance. A strong economic recovery followed and provided initial conditions for further banking development. Our empirical evidence based on firm-level data supports the model’s predictions.

Our model suggests that a financial crisis, though it often causes a credit crunch and a deep economic recession, may have its benefits as well. One of the benefits highlighted in this paper is that if an economy is stuck in a banking trap, in which the financial and real sectors are separated, a crisis may lead it out of the trap and thus bring about a strong economic recovery. This, in turn, also sets the stage for financial development by creating favorable initial conditions. It should be emphasized, however, that whether economic recovery and growth can continue depends critically on whether banking development can be sustained.

Our model has several policy implications for efforts to sustain further banking development. A high priority should be placed on fiscal policy. It is critical that the government harden its budget constraint and avoid creating an environment in which government bonds crowd out bank loans. The economic recovery has clearly provided the conditions in which this could happen: since 1999, the government’s fiscal balance turned into a surplus in Russia as well as in Ukraine. Moreover, reducing the information asymmetry between banks and their borrowers is another key objective. Policies aiming at improving corporate governance, accounting and transparency, and credit risk assessment and management are all necessary. Furthermore, as bank lending grows, an effective enforcement of loan contacts becomes more important, as suggested by Perotti (2002). Finally, our results suggest that in order to sustain banking development, the banks’ returns on loans should be attractive. Thus, at an early stage of bank development, a moderate amount of competition in the banking sector is desirable. If bank competition is too strong, however, it will be difficult to maintain the incentives of banks to lend to the real sector and to invest in evaluating credit risk.
APPENDIX I: Figures
Figure A2. Barter, Bank Lending and the Government Sector

- Bank's Claims on Government in % of GDP
- Government Deficit in % of GDP
- Credit to the Private Sector in % of GDP
- Exchange Rate (US $ in local currency)
- Bank Credit to the Private Sector in % of GDP
- Belarus

Belarus
Figure A3. The International Economy
APPENDIX II: Proofs

Proof of Lemma 2: Given the quality rank of firms, \( \lambda_1 > \lambda_2 > \ldots \lambda_{n-1} > \lambda_n > \ldots > \lambda_N \), without loss of generality, let us start with firm \( n \), which is chosen that for given \( \lambda_N \) and \( s \); this firm will borrow, but all \( n-1 \) better quality firms do not borrow in the lending market. However, the \( n-1 \) firms’ withdrawal from the lending market lowers the average quality of the remaining \( N-n+1 \) firms

\[
\bar{\lambda}_{N-n+1} = \frac{1}{N-n+1} \sum_{i=1}^{N-n+1} \lambda_i
\]

\[
= \frac{(1+N-n+1)\mu}{2}
\]

\[
< \frac{(1+N)\mu}{2}
\]

\[
= \bar{\lambda}_N.
\]

The lower average quality of the pool of borrowing firms may make firm \( n \) decide not to borrow. Given the quality of firm \( n \)

\[
\lambda_n = (N-n+1)\mu
\]

applying Lemma 1, the general condition for firm \( n \) not to borrow is \( \bar{\lambda}_{N-n+1}/\lambda_n \leq \frac{1+s}{b} \), or

\[
\frac{(1+N-n+1)\mu}{2(N-n+1)\mu} \leq \frac{1+s}{b}.
\]

Rewrite the above condition as the following NBF equation

\[
\psi (n) = \frac{b(N-n+2)}{2(N-n+1)} - 1 \leq s.
\]

Where, in general \( \psi (n) \) is defined as

\[
\psi (n) \equiv \frac{\bar{\lambda}_{N-n+1}}{\lambda_n} - 1.
\]

It is easy to see that \( \psi (n) \) is a convex increasing function of \( n \) with \( \psi (0) = \frac{b(N+2)}{2(N+1)} - 1 \) and \( \psi (N) = b - 1 \). Thus, if \( \psi (N) = b - 1 \leq s \), the equilibrium is \( n^* = N \), i.e. no firm borrows.

Furthermore, if \( \psi (0) = \frac{b(N+2)}{2(N+1)} - 1 \geq s \), by Lemma 1, all firms will borrow and the equilibrium is \( n^* = 0 \).

Finally, if \( \psi (0) = \frac{b(N+2)}{2(N+1)} - 1 < s \) and \( \psi (N) = b - 1 > s \), there exists \( n^* \in (0, N) \) that \( \psi (n^*) = s \).

Concerning the stability of the equilibrium, it is easy to see that for any firm \( i \), where \( i \leq n^* \), \( \psi (i) < s (i) \). Thus, firm \( i \) will not borrow from banks which will push more firms to choose not to borrow until \( i = n^* \). Moreover, for any firm \( j \), where \( j > n^* \),
ψ(\(j\)) > s(\(j\)). Thus, firm \(j\) will borrow which pushes more firms to choose to borrow until \(j = n^*\). Thus, \(n^*\) is a stable equilibrium.

Proof of Proposition 3.2: Notice that \(s(n)\) is a linear upward sloping function with \(s(0) = \phi r_o\), and \(s(N) = \frac{\phi r_o R}{R - Nt}\). Moreover, \(\psi(n)\) is a convex upward sloping function with \(\psi(0) = b \frac{N + 2}{2(N + 1)} - 1\), and \(\psi(N) = b - 1\).

If \(s(0) > \psi(0)\) and \(s(N) < \psi(N)\); or if \((b - 1) \frac{1 - \frac{N}{R}}{1 - \frac{N}{R}} > \phi r_o > \frac{b(N + 2)}{2(N + 1)} - 1\), a unique interior equilibrium exists that \(n^* \in (0, N)\) and \(s^* \in (s(0), s(N))\). Rewriting \(s(N) = \frac{\phi r_o R}{R - Nt} \psi(N) = b - 1\) as \((b - 1) \frac{1 - \frac{N}{R}}{1 - \frac{N}{R}} > \phi r_o = s(0)\) and combining with \(s(0) > \psi(0)\) we have the conditions stated in the proposition.

Concerning the stability of the equilibrium \((n^*, s^*)\), it is easy to see that for any firm \(i\), where \(i \leq n^*\), \(\psi(i) < s(i)\). Thus, firm \(i\) will not borrow from banks pushing up \(s\) and leading more firms to choose not to borrow. This makes \(\psi(i)\) increase faster than \(s(i)\) until \(i = n^*\). Moreover, for any firm \(j\), where \(j > n^*\), \(\psi(j) > s(j)\). Thus, firm \(j\) will borrow pushing down \(s\) and leading more firms to choose to borrow. This makes \(\psi(i)\) decrease faster than \(s(i)\) until \(j = n^*\). Thus, \((n^*, s^*)\) is a stable equilibrium. Given that \(s(n)\) increases (decreases) with \(t, \phi r_o R\), the comparative static results follow.

Proof of Proposition 4.2: We are going to show two possible cases when \(\phi\) is reduced to \(\phi'\). Notice that \(\psi(n)\) is independent from \(\phi\); and further notice that \(s(n)\) is a linear increasing function of \(\phi\).

1. If \(\phi'\) is reduced moderately a unique stable interior equilibrium \(n^c \in (0, n^*)\) exists such that \(n^c\) rms barter trade and the number of bartering rms is reduced. This is because with a lower \(\phi'\) that
   \[
   \phi' r_o > \frac{b(N + 2)}{2(N + 1)} - 1.
   \]
   Applying Lemma 1 we have the result.

2. If \(\phi'\) is reduced substantially then in equilibrium \(n^c = 0\), i.e. every rm borrows. This is because with a drastic reduction of \(\phi\) to \(\phi'\) that
   \[
   \frac{\phi' r_o R}{R - tN} < \frac{b(N + 2)}{2(N + 1)} - 1
   \]
   which implies \(s(N) < \psi(0)\), then in equilibrium \(n^c = 0\).
REFERENCES


